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# A NOTE ON INTUITIONISTIC FUZZY $\hat{\beta}$ GENERALIZED IRRESOLUTE MAPPINGS

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**ABSTRACT:** In this paper a new class of mapping called intuitionistic fuzzy  $\hat{\beta}$  generalized irresolute mapping in intuitionistic fuzzy topological space is introduced and its properties are studied. Further the notion of intuitionistic fuzzy  $\hat{\beta}_a T_{1/2}$  space and intuitionistic fuzzy  $\hat{\beta}_b T_{1/2}$  are introduced.

**KEYWORDS:** Intuitionistic fuzzy topology, intuitionistic fuzzy  $\hat{\beta}$  generalized closed set, intuitionistic fuzzy  $\hat{\beta}$  generalized open set, intuitionistic fuzzy  $\hat{\beta}$  generalized irresolute mapping, intuitionistic fuzzy contra  $\hat{\beta}$  generalized irresolute mapping, intuitionistic fuzzy  $\hat{\beta}_a T_{1/2}$  space and intuitionistic fuzzy  $\hat{\beta}_b T_{1/2}$  space.

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## I. INTRODUCTION

After the introduction of Fuzzy set (FS) by Zadeh [12] in 1965 and fuzzy topology by Chang [3] in 1967, several researches were conducted on the generalizations of the notions of fuzzy sets and fuzzy topology. The concept of intuitionistic fuzzy set (IFS) was introduced by Atanassov in 1983 as a generalization of fuzzy sets. In 1997 Coker [4] introduced the concept of intuitionistic fuzzy topological space. In this paper we introduce the notion of intuitionistic fuzzy  $\hat{\beta}$  generalized irresolute mappings, intuitionistic fuzzy contra  $\hat{\beta}$  generalized irresolute mapping in intuitionistic fuzzy topological space and studied some of their properties. We provide some characterizations of intuitionistic fuzzy  $\hat{\beta}$  generalized irresolute mappings, intuitionistic fuzzy contra  $\hat{\beta}$  generalized irresolute mappings and established the relationships with other classes of early defined forms of intuitionistic fuzzy mappings.

## II. PRELIMINARIES

**Definition 2.1:** [1] Let  $X$  be a non empty fixed set. An intuitionistic fuzzy set (IFS in short)  $A$  in  $X$  is an object having the form

$$A = \{ \langle x, \mu_A(x), \nu_A(x) \rangle / x \in X \}$$

where the functions  $\mu_A(x): X \rightarrow [0, 1]$  and  $\nu_A(x): X \rightarrow [0, 1]$  denote the degree of membership (namely  $\mu_A(x)$ ) and the degree of non-membership (namely  $\nu_A(x)$ ) of each element  $x \in X$  to the set  $A$ , respectively, and  $0 \leq \mu_A(x) + \nu_A(x) \leq 1$  for each  $x \in X$ . Denote the set of all intuitionistic fuzzy sets in  $X$  by  $IFS(X)$ .

**Definition 2.2:** [1] Let  $A$  and  $B$  be IFSs of the form  $A = \{ \langle x, \mu_A(x), \nu_A(x) \rangle / x \in X \}$  and  $B = \{ \langle x, \mu_B(x), \nu_B(x) \rangle / x \in X \}$ . Then

- (a)  $A \subseteq B$  if and only if  $\mu_A(x) \leq \mu_B(x)$  and  $\nu_A(x) \geq \nu_B(x)$  for all  $x \in X$
- (b)  $A = B$  if and only if  $A \subseteq B$  and  $B \subseteq A$
- (c)  $A^c = \{ \langle x, \nu_A(x), \mu_A(x) \rangle / x \in X \}$
- (d)  $A \cap B = \{ \langle x, \mu_A(x) \wedge \mu_B(x), \nu_A(x) \vee \nu_B(x) \rangle / x \in X \}$
- (e)  $A \cup B = \{ \langle x, \mu_A(x) \vee \mu_B(x), \nu_A(x) \wedge \nu_B(x) \rangle / x \in X \}$

For the sake of simplicity, we shall use the notation  $A = \langle x, \mu_A, \nu_A \rangle$  instead of  $A = \{ \langle x, \mu_A(x), \nu_A(x) \rangle / x \in X \}$ . Also for the sake of simplicity, we shall use the notation  $A = \{ \langle x, (\mu_A, \mu_B), (\nu_A, \nu_B) \rangle \}$  instead of  $A = \langle x, (A/\mu_A, B/\mu_B), (A/\nu_A, B/\nu_B) \rangle$ .

The intuitionistic fuzzy sets  $0 \sim = \{ \langle x, 0, 1 \rangle / x \in X \}$  and  $1 \sim = \{ \langle x, 1, 0 \rangle / x \in X \}$  are respectively the empty set and the whole set of  $X$ .

**Definition 2.3:** [3] An intuitionistic fuzzy topology (IFT in short) on  $X$  is a family  $\tau$  of IFSs in  $X$  satisfying the following axioms.

- (i)  $0 \sim, 1 \sim \in \tau$
- (ii)  $G_1 \cap G_2 \in \tau$  for any  $G_1, G_2 \in \tau$
- (iii)  $\cup G_i \in \tau$  for any family  $\{ G_i / i \in J \} \subseteq \tau$ .



In this case the pair  $(X, \tau)$  is called an intuitionistic fuzzy topological space (IFTS in short) and any IFS in  $\tau$  is known as an intuitionistic fuzzy open set (IFOS in short) in  $X$ . The complement  $A^c$  of an IFOS  $A$  in IFTS  $(X, \tau)$  is called an intuitionistic fuzzy closed set (IFCS in short) in  $X$ .

**Definition 2.4:[3]** Let  $(X, \tau)$  be an IFTS and  $A = \langle x, \mu_A, \nu_A \rangle$  be an IFS in  $X$ . Then the intuitionistic fuzzy interior and intuitionistic fuzzy closure are defined by  
 $\text{int}(A) = \cup \{ G / G \text{ is an IFOS in } X \text{ and } G \subseteq A \}$ ,  
 $\text{cl}(A) = \cap \{ K / K \text{ is an IFCS in } X \text{ and } A \subseteq K \}$   
 Note that for any IFS  $A$  in  $(X, \tau)$ , we have  $\text{cl}(A^c) = [\text{int}(A)]^c$  and  $\text{int}(A^c) = [\text{cl}(A)]^c$ .

**Definition 2.5: [4]** An IFS  $A = \langle x, \mu_A, \nu_A \rangle$  in an IFTS  $(X, \tau)$  is said to be a  
 (i) intuitionistic fuzzy semi closed set (IFSCS for short) if  $\text{int}(\text{cl}(A)) \subseteq A$ ,  
 (ii) intuitionistic fuzzy pre-closed set (IFPCS for short) if  $\text{cl}(\text{int}(A)) \subseteq A$ ,  
 (iii) intuitionistic fuzzy  $\alpha$ -closed set (IF $\alpha$ CS for short) if  $\text{cl}(\text{int}(\text{cl}(A))) \subseteq A$ ,  
 (iv) intuitionistic fuzzy  $\gamma$ -closed set (IF $\gamma$ CS for short) if  $\text{cl}(\text{int}(A)) \cap \text{int}(\text{cl}(A)) \subseteq A$   
 The respective complements of the above IFCSs are called their respective IFOSs.

The family of all IFSCSs, IFPCSs, IF $\alpha$ CSs and IF $\gamma$ CSs (respectively IFOSOs, IFPOSo, IF $\alpha$ OSs and IF $\gamma$ OSs) of an IFTS  $(X, \tau)$  are respectively denoted by IFSC(X), IFPC(X), IF $\alpha$ C(X) and IF $\gamma$ C(X) (respectively IFSO(X), IFPO(X), IF $\alpha$ O(X) and IF $\gamma$ O(X)).

**Definition 2.6:[11]** Let  $A$  be an IFS in an IFTS  $(X, \tau)$ . Then  
 $\text{sint}(A) = \cup \{ G / G \text{ is an IFOS in } X \text{ and } G \subseteq A \}$ ,  
 $\text{scl}(A) = \cap \{ K / K \text{ is an IFCS in } X \text{ and } A \subseteq K \}$ .  
 Note that for any IFS  $A$  in  $(X, \tau)$ , we have  $\text{scl}(A^c) = (\text{sint}(A))^c$  and  $\text{sint}(A^c) = (\text{scl}(A))^c$ .

**Definition 2.7:[10]** An IFS  $A$  in an IFTS  $(X, \tau)$  is an intuitionistic fuzzy generalized closed set (IFGCS in short) if  $\text{cl}(A) \subseteq U$  whenever  $A \subseteq U$  and  $U$  is an IFOS in  $X$ .

**Definition 2.8:[10]** An IFS  $A$  in an IFTS  $(X, \tau)$  is said to be an intuitionistic fuzzy generalized semi closed set (IFGSCS in short) if  $\text{scl}(A) \subseteq U$  whenever  $A \subseteq U$  and  $U$  is an IFOS in  $(X, \tau)$ .

**Definition 2.9:[10]** An IFS  $A$  is said to be an intuitionistic fuzzy generalized semi open set (IFGSOS in short) in  $X$  if the complement  $A^c$  is an IFGSCS in  $X$ . The family of all IFGSCSs (IFGSOSs) of an IFTS  $(X, \tau)$  is denoted by IFGSC(X) (IFGSO(X)).

**Definition 2.10:[5]** Let  $f$  be a mapping from an IFTS  $(X, \tau)$  into an IFTS  $(Y, \sigma)$ . Then  $f$  is said to be intuitionistic fuzzy

continuous (IF continuous in short) if  $f^{-1}(B) \in \text{IFO}(X)$  for every  $B \in \sigma$ .

**Definition 2.11: [5]** Let  $f$  be a mapping from an IFTS  $(X, \tau)$  into an IFTS  $(Y, \sigma)$ . Then  $f$  is said to be an

- (i) intuitionistic fuzzy semi continuous mapping (IFS continuous mapping for short) if  $f^{-1}(B) \in \text{IFSO}(X)$  for every  $B \in \sigma$
- (ii) intuitionistic fuzzy  $\alpha$ -continuous mapping (IF $\alpha$  continuous mapping for short) if  $f^{-1}(B) \in \text{IF}\alpha\text{O}(X)$  for every  $B \in \sigma$
- (iii) intuitionistic fuzzy pre continuous mapping (IFP continuous mapping for short) if  $f^{-1}(B) \in \text{IFPO}(X)$  for every  $B \in \sigma$
- (iv) intuitionistic fuzzy  $\gamma$  continuous mapping (IF $\gamma$  continuous mapping for short) if  $f^{-1}(B) \in \text{IF}\gamma\text{O}(X)$  for every  $B \in \sigma$ .

**Definition 2.12: [11]** Let  $f$  be a mapping from an IFTS  $(X, \tau)$  into an IFTS  $(Y, \sigma)$ . Then  $f$  is said to be an intuitionistic fuzzy generalized continuous mapping (IFG continuous mapping for short) if  $f^{-1}(B) \in \text{IFGC}(X)$  for every IFCS  $B$  in  $Y$ .

**Definition 2.13: [11]** Let  $f$  be a mapping from an IFTS  $(X, \tau)$  into an IFTS  $(Y, \sigma)$ . Then  $f$  is said to be an intuitionistic fuzzy semi-pre continuous mapping (IFSP continuous mapping for short) if  $f^{-1}(B) \in \text{IFSPO}(X)$  for every  $B \in \sigma$ .

**Result 2.14:[8]** Every IF continuous mapping is an IFG continuous mapping.

**Definition 2.15:[8]** A mapping  $f: (X, \tau) \rightarrow (Y, \sigma)$  is called an intuitionistic fuzzy generalized semi continuous (IFGS continuous in short) if  $f^{-1}(B)$  is an IFGSCS in  $(X, \tau)$  for every IFCS  $B$  of  $(Y, \sigma)$ .

**Definition 2.16: [8]** An IFTS  $(X, \tau)$  is said to be an intuitionistic fuzzy  $\hat{\beta}_a T_{1/2}$  (IF $\hat{\beta}_a T_{1/2}$  in short) space if every IF $\hat{\beta}_a$ GCS in  $X$  is an IFCS in  $X$ .

**Definition 2.17: [8]** An IFTS  $(X, \tau)$  is said to be an intuitionistic fuzzy  $\hat{\beta}_b T_{1/2}$  (IF $\hat{\beta}_b T_{1/2}$  in short) space if every IF $\hat{\beta}_b$ GCS in  $X$  is an IFGCS in  $X$ .

**Definition 2.18:[9]** Let  $f$  be a mapping from an IFTS  $(X, \tau)$  into an IFTS  $(Y, \sigma)$ . Then  $f$  is said to be an intuitionistic fuzzy irresolute (IF irresolute in short) if  $f^{-1}(B) \in \text{IFCS}(X)$  for every IFCS  $B$  in  $Y$ .

**Definition 2.19:[9]** Let  $f$  be a mapping from an IFTS  $(X, \tau)$  into an IFTS  $(Y, \sigma)$ . Then  $f$  is said to be an intuitionistic fuzzy generalized irresolute (IFG irresolute in short) if  $f^{-1}(B) \in \text{IFGCS}(X)$  for every IFGCS  $B$  in  $Y$ .



### III. INTUITIONISTIC FUZZY GENERALIZED IRRESOLUTE MAPPINGS

In this section, we have introduced intuitionistic fuzzy generalized irresolute mappings and studied some of their properties.

**Definition 3.1:** A mapping  $f : (X, \tau) \rightarrow (Y, \sigma)$  is called an intuitionistic fuzzy generalized irresolute (IF $\beta$ G irresolute) mapping if  $f^{-1}(A)$  is an IF $\beta$ GCS in  $(X, \tau)$  for every IF $\beta$ GCS  $A$  of  $(Y, \sigma)$ .

**Theorem 3.2:** If  $f : (X, \tau) \rightarrow (Y, \sigma)$  is an IF $\beta$ G irresolute mapping, then  $f$  is an IF $\beta$ G continuous mapping but not conversely.

**Proof:** Assume that  $f$  is an IF $\beta$ G irresolute mapping. Let  $A$  be any IFCS in  $Y$ . Since every IFCS is an IF $\beta$ GCS,  $A$  is an IF $\beta$ GCS in  $Y$ . By hypothesis  $f^{-1}(A)$  is an IF $\beta$ GCS in  $X$ . Hence  $f$  is an IF $\beta$ G continuous mapping.

**Example 3.3:** Let  $X = \{ a, b \}$ ,  $Y = \{ u, v \}$  and  $G_1 = \langle x, (0.1, 0.3), (0.6, 0.3) \rangle$ ,  $G_2 = \langle y, (0.3, 0.1), (0.5, 0.6) \rangle$ . Then  $\tau = \{ 0., G_1, 1. \}$  and  $\sigma = \{ 0., G_2, 1. \}$  are IFTs on  $X$  and  $Y$  respectively. Define a mapping  $f : (X, \tau) \rightarrow (Y, \sigma)$  by  $f(a) = u$  and  $f(b) = v$ . Then  $f$  is an IF $\beta$ G continuous mapping. Let  $B = \langle y, (0.1, 0.1), (0.6, 0.4) \rangle$  is an IF GCS in  $Y$ . But  $f^{-1}(B) = \langle x, (0.1, 0.1), (0.6, 0.4) \rangle$  is not an IF GCS in  $X$ . Therefore,  $f$  is not an IF G irresolute mapping.

**Theorem 3.4:** If  $f : (X, \tau) \rightarrow (Y, \sigma)$  is an IF $\beta$ G irresolute mapping, then  $f$  is an IFGS continuous mapping but not conversely.

**Proof:** Assume that  $f$  is an IF $\beta$ G irresolute mapping. Let  $A$  be any IFCS in  $Y$ . Since every IFCS is an IF $\beta$ GCS,  $A$  is an IF $\beta$ GCS in  $Y$ . By hypothesis  $f^{-1}(A)$  is an IF $\beta$ GCS in  $X$ . This implies  $f^{-1}(A)$  is an IFGCS in  $X$ . Hence  $f$  is an IFGS continuous mapping.

**Example 3.5:** Let  $X = \{ a, b \}$ ,  $Y = \{ u, v \}$  and  $G_1 = \langle x, (0.1, 0.3), (0.3, 0.3) \rangle$ ,  $G_2 = \langle y, (0.3, 0.1), (0.4, 0.4) \rangle$ . Then  $\tau = \{ 0., G_1, 1. \}$  and  $\sigma = \{ 0., G_2, 1. \}$  are IFTs on  $X$  and  $Y$  respectively. Define a mapping  $f : (X, \tau) \rightarrow (Y, \sigma)$  by  $f(a) = u$  and  $f(b) = v$ . Then  $f$  is an IFGS continuous mapping. Let  $B = \langle y, (0.1, 0.1), (0.3, 0.4) \rangle$  is an IF $\beta$ GCS in  $Y$ . But  $f^{-1}(B) = \langle x, (0.1, 0.1), (0.3, 0.4) \rangle$  is not an IF $\beta$ GCS in  $X$ . Therefore,  $f$  is not an IF G irresolute mapping.

**Theorem 3.6:** If  $f : (X, \tau) \rightarrow (Y, \sigma)$  is an IF $\beta$ G irresolute mapping in an IF $\beta_a T_{1/2}$  space  $X$ , then  $f$  is an IF continuous mapping.

**Proof:** Let  $A$  be an IFCS in  $Y$ . Then  $A$  is an IF GCS in  $Y$ . Since  $f$  is an IF $\beta$ G irresolute,  $f^{-1}(A)$  is an IF $\beta$ GCS in  $X$ . Also, since  $X$  is an IF $\beta_a T_{1/2}$  space,  $f^{-1}(A)$  is an IFCS in  $X$ . Hence  $f$  is an IF continuous mapping.

**Theorem 3.7:** Let  $f : (X, \tau) \rightarrow (Y, \sigma)$  and  $g : (Y, \sigma) \rightarrow (Z, \eta)$  be IF $\beta$ G irresolute mappings. Then  $g \circ f : (X, \tau) \rightarrow (Z, \eta)$  is an IF $\beta$ G irresolute mapping.

**Proof:** Let  $A$  be an IF $\beta$ GCS in  $Z$ . Then by hypothesis,  $g^{-1}(A)$  is an IF $\beta$ GCS in  $Y$ . Since  $f$  is an IF $\beta$ G irresolute mapping,  $f^{-1}(g^{-1}(A))$  is an IF $\beta$ GCS in  $X$ . Thus,  $(g \circ f)^{-1}(A)$  is an IF $\beta$ GCS in  $X$ . Therefore  $g \circ f$  is an IF $\beta$ G irresolute mapping.

**Theorem 3.8:** Let  $f : (X, \tau) \rightarrow (Y, \sigma)$  be an IF $\beta$ G irresolute mapping and  $g : (Y, \sigma) \rightarrow (Z, \eta)$  be an IF $\beta$ G continuous mapping. Then  $g \circ f : (X, \tau) \rightarrow (Z, \eta)$  is an IF $\beta$ G continuous mapping.

**Proof:** Let  $A$  be an IFCS in  $Z$ . Then by hypothesis,  $g^{-1}(A)$  is an IF GCS in  $Y$ . Since  $f$  is an IF $\beta$ G irresolute mapping,  $f^{-1}(g^{-1}(A))$  is an IF $\beta$ GCS in  $X$ . Thus,  $(g \circ f)^{-1}(A)$  is an IF $\beta$ GCS in  $X$ .

Therefore,  $g \circ f$  is an IF G continuous mapping.

**Theorem 3.9:** If  $f : (X, \tau) \rightarrow (Y, \sigma)$  is an IF $\beta$ G irresolute mapping in an IF $\beta_b T_{1/2}$  space in  $X$ , then  $f$  is an IFG irresolute mapping.

**Proof:** Let  $A$  be an IFGCS in  $Y$ . Then  $A$  is an IF $\beta$ GCS in  $Y$ . Therefore  $f^{-1}(A)$  is an IF $\beta$ GCS in  $X$ , by hypothesis. Since  $X$  is an IF $\beta_b T_{1/2}$  space,  $f^{-1}(A)$  is an IFGCS in  $X$ . Hence  $f$  is an IFG irresolute mapping.

**Theorem 3.10:** Let  $f : (X, \tau) \rightarrow (Y, \sigma)$  be a mapping from an IFTS  $X$  into an IFTS  $Y$ . Then the following conditions are equivalent if  $X$  and  $Y$  are IF $\beta_a T_{1/2}$  spaces:

- (i)  $f$  is an IF $\beta$ G irresolute mapping
- (ii)  $f^{-1}(B)$  is an IF $\beta$ GOS in  $X$  for each IF $\beta$ GOS in  $Y$
- (iii)  $cl(f^{-1}(B)) \subseteq f^{-1}(cl(B))$  for each IFS  $B$  of  $Y$ .

**Proof:(i)  $\Rightarrow$  (ii):** Obviously true.

**(ii)  $\Rightarrow$  (iii):** Let  $B$  be any IFS in  $Y$ . Clearly  $B \subseteq cl(B)$ . Then  $f^{-1}(B) \subseteq f^{-1}(cl(B))$ . Since  $cl(B)$  is an IFCS in  $Y$ ,  $cl(B)$  is an IF $\beta$ GCS in  $Y$ . Therefore,  $f^{-1}(cl(B))$  is an IF $\beta$ GCS in  $X$ , by hypothesis. Since  $X$  is an IF $\beta_a T_{1/2}$  space,  $f^{-1}(cl(B))$  is an IFCS



in  $X$ . Hence  $\text{cl}(f^{-1}(B)) \subseteq \text{cl}(f^{-1}(\text{cl}(B))) = f^{-1}(\text{cl}(B))$ . That is  $\text{cl}(f^{-1}(B)) \subseteq f^{-1}(\text{cl}(B))$ .

(iii)  $\Rightarrow$  (i): Let  $B$  be an  $\text{IF}_{\beta}^{\beta}\text{GCS}$  in  $Y$ . Since  $Y$  is an  $\text{IF}_{\beta}^{\beta}T_{1/2}$  space,  $B$  is an IFCS in  $Y$  and  $\text{cl}(B) = B$ . Hence  $f^{-1}(B) = f^{-1}(\text{cl}(B)) \supseteq \text{cl}(f^{-1}(B))$ , by hypothesis. But clearly  $f^{-1}(B) \subseteq \text{cl}(f^{-1}(B))$ . Therefore,  $\text{cl}(f^{-1}(B)) = f^{-1}(B)$ . This implies  $f^{-1}(B)$  is an IFCS in  $X$  and hence it is an  $\text{IF}_{\beta}^{\beta}\text{GCS}$  in  $X$ . Thus  $f$  is an  $\text{IF}_{\beta}^{\beta}\text{G}$  irresolute mapping.

#### IV. INTUITIONISTIC FUZZY CONTRA GENERALIZED IRRESOLUTE MAPPINGS

In this section, we have introduced intuitionistic fuzzy contra  $\beta$  generalized irresolute mapping and studied some of its properties.

**Definition 4.1:** A mapping  $f : (X, \tau) \rightarrow (Y, \sigma)$  is called an intuitionistic fuzzy contra  $\beta$  generalized irresolute (IFC $\beta$ G irresolute in short) mapping if  $f^{-1}(A)$  is an  $\text{IF}_{\beta}^{\beta}\text{GCS}$  in  $(X, \tau)$  for every  $\text{IF}_{\beta}^{\beta}\text{GOS}$   $A$  of  $(Y, \sigma)$ .

**Theorem 4.2:** If  $f : (X, \tau) \rightarrow (Y, \sigma)$  is an IFC $\beta$ G irresolute mapping, then  $f$  is an IFC $\beta$ G continuous mapping but not conversely.

**Proof:** Let  $f$  be an IFC $\beta$ G irresolute mapping. Let  $A$  be any IFCS in  $Y$ . Since every IFCS is an  $\text{IF}_{\beta}^{\beta}\text{GCS}$ ,  $A$  is an  $\text{IF}_{\beta}^{\beta}\text{GCS}$  in  $Y$ . By hypothesis  $f^{-1}(A)$  is an  $\text{IF}_{\beta}^{\beta}\text{GOS}$  in  $X$ . Hence  $f$  is an IFC $\beta$ G continuous mapping.

**Example 4.3:** Let  $X = \{a, b\}$ ,  $Y = \{u, v\}$  and  $G_1 = \langle x, (0.1, 0.3), (0.6, 0.3) \rangle$ ,  $G_2 = \langle y, (0.5, 0.6), (0.3, 0.1) \rangle$ . Then  $\tau = \{0_-, G_1, 1_-\}$  and  $\sigma = \{0_-, G_2, 1_-\}$  are IFTs on  $X$  and  $Y$  respectively. Define a mapping  $f : (X, \tau) \rightarrow (Y, \sigma)$  by  $f(a) = u$  and  $f(b) = v$ . Then  $f$  is an IFC $\beta$ G continuous mapping but  $f$  is not an IFC $\beta$ G irresolute mapping, since  $B = \langle y, (0.1, 0.1), (0.6, 0.4) \rangle$  is an  $\text{IF}_{\beta}^{\beta}\text{GOS}$  in  $Y$  but  $f^{-1}(B) = \langle x, (0.1, 0.1), (0.6, 0.4) \rangle$  is not an  $\text{IF}_{\beta}^{\beta}\text{GCS}$  in  $X$ .

**Theorem 4.4:** Let  $f : (X, \tau) \rightarrow (Y, \sigma)$  be an IFC $\beta$ G irresolute mapping, then  $f^{-1}(A)$  is an IFGSCS in  $X$  for every IFOS  $A$  in  $Y$  but not conversely.

**Proof:** Let  $f$  be an IFC $\beta$ G irresolute mapping. Let  $A$  be any IFOS in  $Y$ . Since every IFOS is an  $\text{IF}_{\beta}^{\beta}\text{GOS}$ ,  $A$  is an  $\text{IF}_{\beta}^{\beta}\text{GOS}$  in  $Y$ . By hypothesis,  $f^{-1}(A)$  is an  $\text{IF}_{\beta}^{\beta}\text{GCS}$  in  $X$ . This implies  $f^{-1}(A)$  is an IFGSCS in  $X$ .

**Example 4.5:** Let  $X = \{a, b\}$ ,  $Y = \{u, v\}$  and  $G_1 = \langle x, (0.1, 0.3), (0.3, 0.3) \rangle$ ,  $G_2 = \langle y, (0.4, 0.4), (0.3, 0.1) \rangle$ . Then  $\tau = \{0_-, G_1, 1_-\}$  and  $\sigma = \{0_-, G_2, 1_-\}$  are IFTs on  $X$  and  $Y$  respectively. Define a mapping  $f : (X, \tau) \rightarrow (Y, \sigma)$  by  $f(a) = u$  and  $f(b) = v$ . Then  $f^{-1}(A)$  is an IFGSCS in  $X$  for every IFOS  $A$  in  $Y$ . But  $f$  is not an IFC $\beta$ G irresolute mapping, since  $B = \langle y, (0.3, 0.4), (0.1, 0.1) \rangle$  is an  $\text{IF}_{\beta}^{\beta}\text{GOS}$  in  $Y$  but  $f^{-1}(B) = \langle x, (0.3, 0.4), (0.1, 0.1) \rangle$  is not an  $\text{IF}_{\beta}^{\beta}\text{GCS}$  in  $X$ .

**Theorem 4.6:** If  $f : (X, \tau) \rightarrow (Y, \sigma)$  is an IFC $\beta$ G irresolute mapping, then  $f$  is an IF contra continuous mapping if  $X$  is an  $\text{IF}_{\beta}^{\beta}T_{1/2}$  space.

**Proof:** Let  $A$  be an IFCS in  $Y$ . Then  $A$  is an  $\text{IF}_{\beta}^{\beta}\text{GCS}$  in  $Y$ . Therefore  $f^{-1}(A)$  is an  $\text{IF}_{\beta}^{\beta}\text{GOS}$  in  $X$ , by hypothesis. Since  $X$  is an  $\text{IF}_{\beta}^{\beta}T_{1/2}$  space,  $f^{-1}(A)$  is an IFOS in  $X$ . Hence  $f$  is an IF contra continuous mapping.

**Theorem 4.7:** If  $f : (X, \tau) \rightarrow (Y, \sigma)$  and  $g : (Y, \sigma) \rightarrow (Z, \eta)$  are IFC $\beta$ G irresolute mappings, then  $g \circ f : (X, \tau) \rightarrow (Z, \eta)$  is an IFC $\beta$ G irresolute mapping.

**Proof:** Let  $A$  be an  $\text{IF}_{\beta}^{\beta}\text{GCS}$  in  $Z$ . Then  $g^{-1}(A)$  is an  $\text{IF}_{\beta}^{\beta}\text{GOS}$  in  $Y$ . Since  $f$  is an IFC $\beta$ G irresolute mapping,  $f^{-1}(g^{-1}(A))$  is an  $\text{IF}_{\beta}^{\beta}\text{GCS}$  in  $X$ . That is  $(g \circ f)^{-1}(A)$  is an  $\text{IF}_{\beta}^{\beta}\text{GCS}$  in  $X$ . Hence  $g \circ f$  is an IFC $\beta$ G irresolute mapping.

**Theorem 4.8:** If  $f : (X, \tau) \rightarrow (Y, \sigma)$  is an IFC $\beta$ G irresolute mapping and  $g : (Y, \sigma) \rightarrow (Z, \eta)$  is an IFC $\beta$ G continuous mapping, then  $g \circ f : (X, \tau) \rightarrow (Z, \eta)$  is an IFC $\beta$ G continuous mapping.

**Proof:** Let  $A$  be an IFCS in  $Z$ . Then by hypothesis,  $g^{-1}(A)$  is an  $\text{IF}_{\beta}^{\beta}\text{GOS}$  in  $Y$ . Since  $f$  is an IFC $\beta$ G irresolute mapping,  $f^{-1}(g^{-1}(A))$  is an  $\text{IF}_{\beta}^{\beta}\text{GCS}$  in  $X$ . That is  $(g \circ f)^{-1}(A)$  is an  $\text{IF}_{\beta}^{\beta}\text{GCS}$  in  $X$ . Hence  $g \circ f$  is an IFC $\beta$ G continuous mapping.

**Theorem 4.9:** If  $f : (X, \tau) \rightarrow (Y, \sigma)$  is an IFC $\beta$ G irresolute mapping and  $g : (Y, \sigma) \rightarrow (Z, \eta)$  is an IFC $\beta$ G continuous mapping, then  $g \circ f : (X, \tau) \rightarrow (Z, \eta)$  is an IFC $\beta$ G continuous mapping.

**Proof:** Let  $A$  be an IFCS in  $Z$ . Then by hypothesis  $g^{-1}(A)$  is an  $\text{IF}_{\beta}^{\beta}\text{GOS}$  in  $Y$ . Since  $f$  is an IFC $\beta$ G irresolute mapping,  $f^{-1}(g^{-1}(A))$  is an  $\text{IF}_{\beta}^{\beta}\text{GOS}$  in  $X$ . That is  $(g \circ f)^{-1}(A)$  is an  $\text{IF}_{\beta}^{\beta}\text{GOS}$  in  $X$ . Hence  $g \circ f$  is an IFC $\beta$ G continuous mapping.

**Theorem 4.10:** Let  $f : (X, \tau) \rightarrow (Y, \sigma)$  and  $g : (Y, \sigma) \rightarrow (Z, \eta)$  be any two mappings. If the mapping  $g \circ f$  is an IFC $\beta$ G irresolute mapping and  $X$  is an  $\text{IF}_{\beta}^{\beta}T_{1/2}$  space, then

- (i)  $(g \circ f)^{-1}(B)$  is an  $\text{IF}_{\beta}^{\beta}\text{GOS}$  in  $X$  for each  $\text{IF}_{\beta}^{\beta}\text{GCS}$  in  $Z$



(ii)  $cl((g \circ f)^{-1}(int(B))) \subseteq (g \circ f)^{-1}(B)$  for each IFS B of Z.

**Proof:(i):** Let B be an  $IF_{\beta}GCS$  in Z. Then  $B^c$  is an  $IF_{\beta}GOS$  in Z. By hypothesis,  $B^c$  is an  $IF_{\beta}GCS$  in X. This implies B is an  $IF_{\beta}GOS$  in X. Hence  $(g \circ f)^{-1}(B)$  is an  $IF_{\beta}GOS$  in X.

**(ii):** Let B be any IFS in Z and  $int(B) \subseteq B$ . Then  $(g \circ f)^{-1}(int(B)) \subseteq (g \circ f)^{-1}(B)$ . Since  $int(B)$  is an IFOS in Z,  $int(B)$  is an  $IF_{\beta}GOS$  in Z. Therefore  $(g \circ f)^{-1}(int(B))$  is an  $IF_{\beta}GCS$  in X, by hypothesis. Since X is an  $IF_{\beta}T_{1/2}$  space,  $(g \circ f)^{-1}(int(B))$  is an IFCS in X. Hence  $cl((g \circ f)^{-1}(int(B))) = (g \circ f)^{-1}(int(B)) \subseteq (g \circ f)^{-1}(B)$ . Therefore,  $cl((g \circ f)^{-1}(int(B))) \subseteq (g \circ f)^{-1}(B)$  for each IFS B of Z.

## V. CONCLUSION

In this paper we introduced the notion of intuitionistic fuzzy  $\beta$  generalized irresolute mappings, intuitionistic fuzzy contra  $\beta$  generalized irresolute mapping in intuitionistic fuzzy topological space and studied some of their properties.

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