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# SIGNED MULTIPLICATION USING QUAD PAIR RECODING

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**Abstract – The main objective of this paper is to reduce the number of partial products obtained during the multiplication. Reducing the number of partial product leads to complete the multiplication process faster. In other words, the elapsed time to complete the multiplication process is reduced. This can be achieved by using Quad pair recoding technique in which multiplier (one of the input of the multiplication process) is coded by using quad pair recoding. Also this method is compared with the existing two methods using recoding and bit pair recoding technique.**

**Keywords: Recoding, Bit Pair Recoding, Quad Pair Recoding**

## I. INTRODUCTION

Generally, multiplication can take atleast two inputs namely multiplicand and multiplier. Each bit in the multiplier is multiplied with the multiplicand and forms a partial product. The partial product is defined as the intermediate product which produced during the multiplication process. Finally all the partial products are summed together to form a final product. In an article written by Andrew. D. Booth (1951), Booth's multiplication is proposed in which multiplication of multiplicand with the bit pair 00 or 11 of the multiplier leads to all 0's as the partial product, 01 leads to multiplicand as the partial product and 10 leads to two's complement of multiplicand as the partial product.

In an article written by Macsorley. O. L (1961), the high speed arithmetic is proposed in which multiplication can be done by variable length shift. This paper the multiplicand or negative multiplicand can be shifted in variable length. This because we have various operation occurred during multiplication. This paper has done the pairing of three bits of multiplier and forms eight operation depending on code. The operations are +0, +2, +2, +4, -4, -2, -2 and 0 for 000, 001, 010, 011, 100, 101, 110, and 111 respectively. Here, +0 represent the zero as a partial product, +2 represent multiplicand without shift, +4 represent multiplicand with one shift, -2 represent negative multiplicand without shift and -4 negative multiplicand with one shift. Similarly this paper has done the pairing of four bits of multiplier and forms sixteen operation depending on code.

In an article written by Louis P. Rubinfeld et al (1975), modified Booth algorithm using bit pair recoding technique is explained. In this, recoded multiplier is formed by grouping three bits and given the code for the corresponding group. In an article written by Carl Hamacher et al (2012), the two methods of signed multiplication is explained namely recoding and bit pair recoding. In this, it is clear that the multiplication done using bit pair recoding has less number of partial product compared to recoding method.

In an article written by Barun Biswas et al (2013), the classical Booth Multiplication method is proposed in which number of partial products required are 4 and 6 for 12 bit and 16 bit multiplication respectively. We know that the partial product formed during multiplication can be summed together to form a final product. Hence the adder circuit is necessary to complete the multiplication process. In an article written by Divya Govekar et al (2017), modified Booth's algorithm using bit pair recoding with two different adders namely CLA and hybrid adders was implemented. In this hybrid adder requires very less number of components and less delay compared to CLA. In an article written by Balakumaran R et al (2016), modified Booth algorithm using bit pair recoding is implemented with CLA and hybrid CLA. In this hybrid CLA takes less delay compared to CLA.

In an article written by Chiou-Yng Lee et al (2005), Low-complexity bit-parallel dual basis multipliers using the modified Booth's algorithm was proposed. This paper achieves 9% space complexity compared to other multipliers. In an article written by Nirlakalla Ravi et al (2012), a new reduced multiplication Structure is proposed using modified Booth Encoding Multiplier for Low power and Low area. This paper modifies the adder used in the multiplier. Normally, Ripple Carry adder is used in the multiplier structure, but here Carry Save adder is proposed. As a result, average power in milliwatt is reduced from 2.99 to 2.84.

In an article written by Vignesh Kumar. R et al (2012), high accuracy fixed width multiplier is designed using radix 4 modified Booth Algorithm. This paper result in significant improvement in area and power when compared to conventional multipliers.





0            -1            0            +1

Now perform multiplication of multiplicand and recoded code of multiplier as follow:

|   |   |   |   |   |   |   |   |   |   |   |   |   |    |   |   |    |
|---|---|---|---|---|---|---|---|---|---|---|---|---|----|---|---|----|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1  | 1 | 0 | 0  |
|   |   |   |   |   |   |   |   |   |   |   |   | 0 | -1 | 0 |   | +1 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1  | 1 | 0 | 0  |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0  | 0 | 0 | 0  |
| 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |    |   |   |    |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |   |   |   |    |   |   |    |
| 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1  | 1 | 0 | 0  |

Since MSB bit of the result is 1, the result is the negative value and the decimal value is obtained by taking two's complement of the result and put negative sign in front of it. Hence the result is  $(-0000001110000011 + 1)_2 = (-0000001110000100)_2 = (-900)_{10}$ . Here we seen that the number of partial product required is only 4 for 8-bit multiplication process, which is nothing but only half of the partial product required when compared to recoding method.

III. PROPOSED METHOD

This section deals with how multiplication can be done using the proposed quad pair recoding method with a suitable example.

3.1 Quad Pair Recoding Method

Quad pair recoding can be obtained directly from the multiplier without forming a recoded code or bit pair recoded code. For that, we first appending of one zero at the *LSB* - 1 position of the multiplier is to be done and then group the bits in five from the left with overlapping. That is first group is formed by taking *LSB* + 3 to *LSB* - 1 bits, second group is formed by taking *LSB* + 7 and *LSB* + 3 bits, third group is formed by taking *LSB* + 11 and *LSB* + 7 bits. After grouping the bit, each pair is assigned a code as shown in table 4.

Table 4 Code using Quad Pair Recoding Method

| Bits  | Code | Bits  | Code |
|-------|------|-------|------|
| 00000 | 0    | 01000 | +1   |
| 00001 | +1   | 01001 | +2   |
| 00010 | +1   | 01010 | +2   |
| 00011 | +2   | 01011 | +3   |
| 00100 | +1   | 01100 | +2   |
| 00101 | +2   | 01101 | +3   |
| 00110 | +2   | 01110 | +3   |
| 00111 | +3   | 01111 | +4   |
| 10000 | -4   | 11000 | -3   |
| 10001 | -3   | 11001 | -2   |
| 10010 | -3   | 11010 | -2   |

| Bits  | Code | Bits  | Code |
|-------|------|-------|------|
| 10011 | -2   | 11011 | -1   |
| 10100 | -3   | 11100 | -2   |
| 10101 | -2   | 11101 | -1   |
| 10110 | -2   | 11110 | -1   |
| 10111 | -1   | 11111 | 0    |

For example, let us assume to perform the multiplication between 60 and -15. Here Multiplicand is  $60_{10} = (00111100)_2$  and Multiplier is  $(-15)_{10} = (11110001)_2$ .

Quad pair Recoding of Multiplier is as follow:

|       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| 7     | 6     | 5     | 4     | 3     | 2     | 1     | 0     | -1       |
| $B_7$ | $B_6$ | $B_5$ | $B_4$ | $B_3$ | $B_2$ | $B_1$ | $B_0$ | $B_{-1}$ |
| 1     | 1     | 1     | 1     | 0     | 0     | 0     | 1     | 0        |
|       |       |       | 11100 |       |       |       | 00010 |          |
|       |       |       | -2    |       |       |       | +1    |          |

Now perform multiplication of multiplicand and recoded code of multiplier as follow:

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
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|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

Since MSB bit of the result is 1, the result is the negative value and the decimal value is obtained by taking two's complement of the result and put negative sign in front of it. Hence the result is  $(-0000001110000011 + 1)_2 = (-0000001110000100)_2 = (-900)_{10}$ . Here we seen that the number of partial product required is only 2 for 8-bit multiplication process, which is nothing but only half of the partial product required when compared to bit pair recoding method and quarter of the partial product required when compared to recoding method.

IV. RESULTS AND DISCUSSION

The performance of this paper is in the number of partial product. Table 5 shows the number of partial product occur in both existing (Recoding and Bit pair Recoding method) and proposed method (Quad Pair Recoding method). From the table 5, it is clear that the number of partial product required in quad pair recoding is half of the partial product required for bit pair recoding and quarter of the partial product required for recoding method.

Figure 1 shows that the variation of number of bits versus number of partial product in all the methods such as recoding, bit pair recoding and quad pair recoding. From the figure 1 also, it is clear that the number of partial product required in quad pair recoding is half of the partial product



required for bit pair recoding and quarter of the partial product required for recoding method.

Table 6 shows that the time required to complete the multiplication process. It is clear that time required to complete the multiplication process is less in quad pair recoding compared to both recoding and bit pair recoding method.

Table 5 Number of Partial Product in each method

| Number of bits | Number of Partial Products |                          |                           |
|----------------|----------------------------|--------------------------|---------------------------|
|                | Existing Methods           |                          | Proposed Method           |
|                | Recoding Method            | Bit pair Recoding Method | Quad Pair Recoding Method |
| 8              | 8                          | 4                        | 2                         |
| 12             | 12                         | 6                        | 3                         |
| 16             | 16                         | 8                        | 4                         |
| 20             | 20                         | 10                       | 5                         |
| 24             | 24                         | 12                       | 6                         |

Table 6 Elapsed Time in each method

| Number of bits | Number of Partial Products |                          |                           |
|----------------|----------------------------|--------------------------|---------------------------|
|                | Existing Methods           |                          | Proposed Method           |
|                | Recoding Method            | Bit pair Recoding Method | Quad Pair Recoding Method |
| 8              | 0.358981                   | 0.014963                 | 0.023797                  |
| 12             | 0.001238                   | 0.001006                 | 0.000979                  |
| 16             | 0.001837                   | 0.000813                 | 0.000866                  |
| 20             | 0.001654                   | 0.001194                 | 0.000976                  |
| 24             | 0.001864                   | 0.001534                 | 0.000836                  |

Figure 2 shows the variation of Elapsed time to complete the multiplication using recoding, bit pair recoding and quad pair recoding. From the figure 2, it is clear that the elapsed time is very less in quad pair recoding compared to bit pair recoding and recoding method when number of bits is larger than 12 bit.

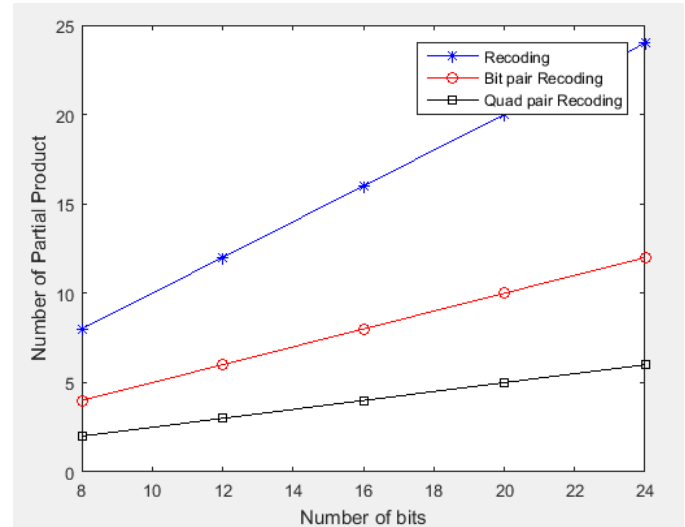


Figure 1 Variation of Number of Partial Products

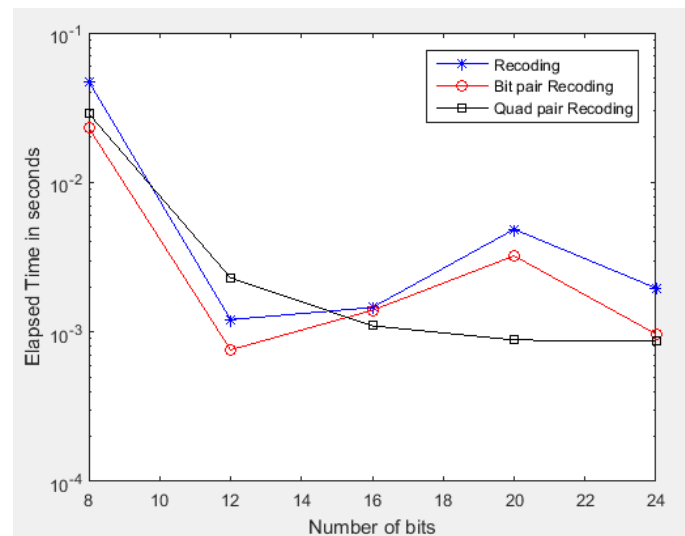


Figure 2 Elapsed Time to complete the multiplication using recoding, bit pair recoding and quad pair recoding

## V. CONCLUSION

This paper achieves a main objective that to reduce the number of partial product. The objective of reducing partial product is that to complete the multiplication faster within a stipulated time. This paper compares the number of partial products required to complete the multiplication using quad pair recoding with recoding and bit pair recoding method and achieves better performance. This paper also compares the elapsed time to complete the multiplication process using quad pair recoding and achieves better performance. Hence, finally it is concluded that the proposed quad pair recoding method performs better in terms of both number of partial products and elapsed time.



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